

①

$$f(x, y, z) = xyz + xy'z + xyz' + x'y'z'$$

	x	x'	
z	*	*	
z'	*	*	
y			
y'			

*	*
*	*

*	*	*	*
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PI: xy , xz , $x'y'z'$

$$MDNF(f) = xy + xz + x'y'z'$$

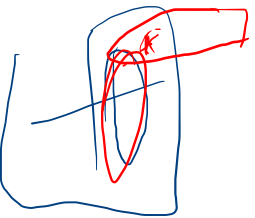
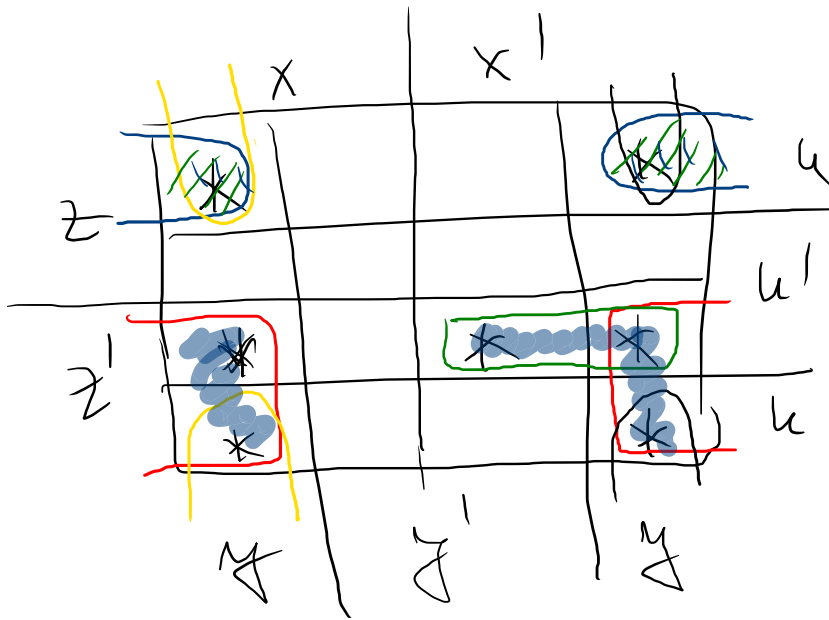
②

	x	x'	
z	*	*	
z'	*	*	
y			
y'			

PI: $x'y$, $x'z'$, yz

$$MDNF(f) = x'z' + yz$$

(3)



$$P1: yz', yz, x'z'u', x'y, x'y, x'yu$$

$$MDNF(t) = yz' + x'z'u' + yz$$

(4)

$\star$	a	b	c
a	a	b	c
b	b	b	a
c	c	a	c

$$G = \{a, b, c\}$$

$$(a \star b) \star c = a \star (b \star c)$$

$$(a \star b) \star c = b \star c = a \quad \checkmark$$

$$a \star (b \star c) = a \star a = a$$

$$(c \star a) \star b = c \star b = a \quad \checkmark$$

$$c \star (a \star b) = c \star b = a$$

⑤

$$f(x) = \ln \frac{1}{1+x^2}$$

$$f: A \rightarrow B$$

$$\frac{1}{1+x^2} > 0 \quad \forall$$

$$A = \mathbb{R}$$

$$\frac{1}{2} = x \Rightarrow 1 = 2x$$

$$2 = \frac{1}{x}$$

$$f(1) = \ln \frac{1}{2} \quad \text{Huge "1-1"}$$

$$f(-1) = \ln \frac{1}{2}$$

$$y = \ln \frac{1}{1+x^2}$$

$$\frac{1}{1+x^2} = e^y \Rightarrow 1 = e^y(1+x^2)$$

$$1+x^2 = \frac{1}{e^y}$$

$$x^2 = \frac{1}{e^y} - 1$$

$$x^2 = \frac{1-e^y}{e^y}$$

$$x = \pm \sqrt{\frac{1-e^y}{e^y}}$$

$$\frac{1-e^y}{e^y} \geq 0$$

$$1-e^y \geq 0$$

$$e^y \leq 1$$

$$e^y \leq e^0$$

$$y \leq 0$$

$$B = (-\infty, 0]$$

$$\textcircled{6} \quad \int \frac{x^2}{\sqrt{1-x-3x^2}} dx = (Ax+B) \cdot \sqrt{1-x-3x^2} + \lambda \int \frac{1}{\sqrt{1-x-3x^2}} dx \quad /$$

$$\frac{x^2}{\sqrt{1-x-3x^2}} = A \sqrt{1-x-3x^2} + (Ax+B) \frac{1}{2\sqrt{1-x-3x^2}} \cdot (-1-6x) + \lambda \frac{1}{\sqrt{1-x-3x^2}}$$

$$x^2 = A(1-x-3x^2) + (Ax+B) \cdot \frac{1}{2}(-1-6x) + \lambda \quad /2$$

$$2x^2 = 2A - 2Ax - 6Ax^2 - Ax - 6Ax^2 - B - 6Bx + \lambda$$

$$2x^2 = -12Ax^2 + (-3A-6B)x + 2A - B + \lambda$$

$$-12A = 2$$

$$-3A - 6B = 0$$

$$2A - B + \lambda = 0$$

$$\boxed{A = -\frac{1}{6}}$$

$$\boxed{B = \frac{1}{12}}$$

$$\boxed{\lambda = \frac{1}{12} + \frac{4}{12} = \frac{5}{12}}$$

$$\int \frac{x^2}{\sqrt{1-x-3x^2}} dx = \left(-\frac{1}{6}x + \frac{1}{12} \right) + \frac{5}{12} \left[\int \frac{1}{\sqrt{1-x-3x^2}} dx \right]$$

$$\begin{aligned} 1-x-3x^2 &= -3 \left(x^2 + \frac{1}{3}x - \frac{1}{3} \right) \\ &= -3 \left(x^2 + 2 \cdot x \cdot \frac{1}{6} + \frac{1}{36} - \frac{1}{36} - \frac{1}{3} \right) \\ &= -3 \left(\left(x + \frac{1}{6} \right)^2 - \frac{13}{36} \right) \\ &= 3 \left(\frac{13}{36} - \left(x + \frac{1}{6} \right)^2 \right) \end{aligned}$$

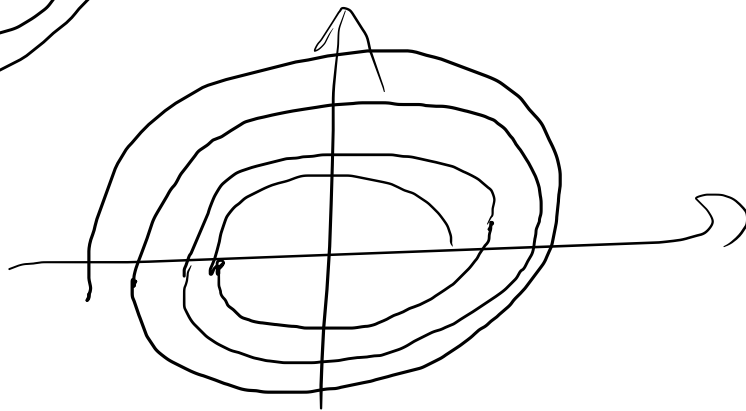
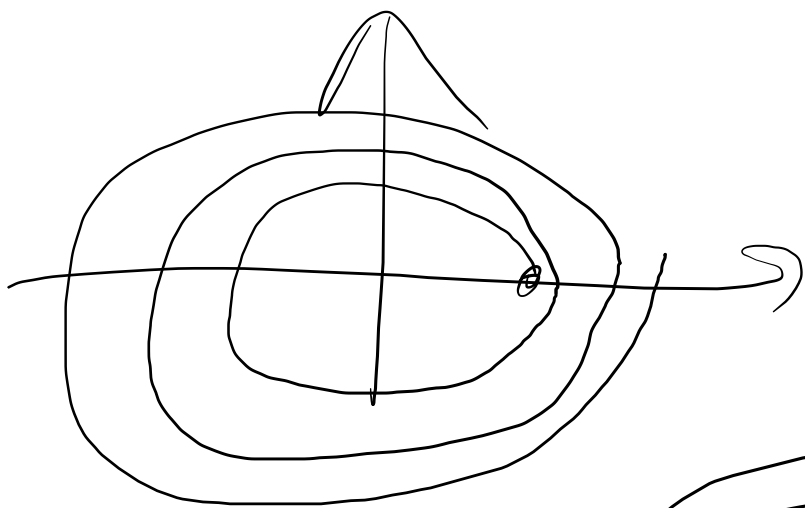
$$\int \frac{1}{\sqrt{1-x-3x^2}} dx = \int \frac{dx}{\sqrt{3 \left(\frac{13}{36} - \left(x + \frac{1}{6} \right)^2 \right)}} = \frac{1}{\sqrt{3}} \int \frac{dt}{\sqrt{\frac{13}{6} - t^2}} = \frac{1}{\sqrt{3}} \arcsin \frac{t}{\frac{\sqrt{13}}{6}} + C$$

$x + \frac{1}{6} = t \quad dx = dt$

$$64 e^{-5\pi i} = 64 e^{-\pi i} = 64 e^{\pi i}$$

$$64 e^{8\pi i} = 64$$

$$e^{16\pi i} = e^0 = 1$$



$$e^{-5\pi i} = e^{-\pi i}$$

$$\frac{0}{0}, \frac{\infty}{\infty}$$

$$\lim_{x \rightarrow x_0} \frac{f(x)}{g(x)} = \lim_{x \rightarrow x_0} \frac{f'(x)}{g'(x)}$$

$$\begin{array}{l} 0 \cdot \infty \\ \lim_{x \rightarrow 0} x \cdot \ln x \end{array} \xrightarrow{\frac{0}{0}} \lim_{x \rightarrow 0} \frac{\ln x}{x^{-1}} \xrightarrow{\frac{\infty}{\infty}} \lim_{x \rightarrow 0} \frac{\frac{1}{x}}{-\frac{1}{x^2}} = 0$$

$$\begin{array}{l} \infty - \infty \\ \lim_{x \rightarrow 0} \left(\frac{1}{x} - \frac{1}{\sin x} \right) \end{array} \xrightarrow{\frac{\infty}{\infty}} \lim_{x \rightarrow 0} \frac{\sin x - x}{x \sin x} \quad \frac{0}{0}$$

$$1^\infty, 0^0, \infty^0: \quad \boxed{\lim_{x \rightarrow 0} (\sin x)^x = A} \quad / \ln$$

$$\ln A = \ln \lim_{x \rightarrow 0} (\sin x)^x = \lim_{x \rightarrow 0} \ln (\sin x)^x = \lim_{x \rightarrow 0} x \ln (\sin x) \xrightarrow{0 \cdot \infty} \lim_{x \rightarrow 0} \frac{\ln (\sin x)}{\frac{1}{x}} = \lim_{x \rightarrow 0} \frac{\frac{\cos x}{\sin x}}{-\frac{1}{x^2}}$$

$$y = \frac{x}{x-2}$$

1) D: $x-2 \neq 0$
 $x \neq 2$

$$D = \mathbb{R} \setminus \{2\}$$

2, $y=0 \quad x=0$
 $x=0 \quad y=0$

3, $y > 0$

$$\frac{x}{x-2} > 0$$

	0	2
x	-	+
x-2	-	+
	+	-

$$y > 0 \quad x \in (-\infty, 0) \cup (2, +\infty)$$

$$y < 0 \quad x \in (0, 2)$$

4, m-m

5, v.A.

$$\lim_{x \rightarrow 2^-} \frac{x}{x-2} = \frac{2}{0^-} = -\infty$$

$$\lim_{x \rightarrow 2^+} \frac{x}{x-2} = \frac{2}{0^+} = +\infty$$

H.A.

$$\lim_{x \rightarrow \pm\infty} \frac{x}{x-2} = \lim_{x \rightarrow \pm\infty} \frac{1}{1} = 1$$

$$y=1 \text{ H.A.}$$

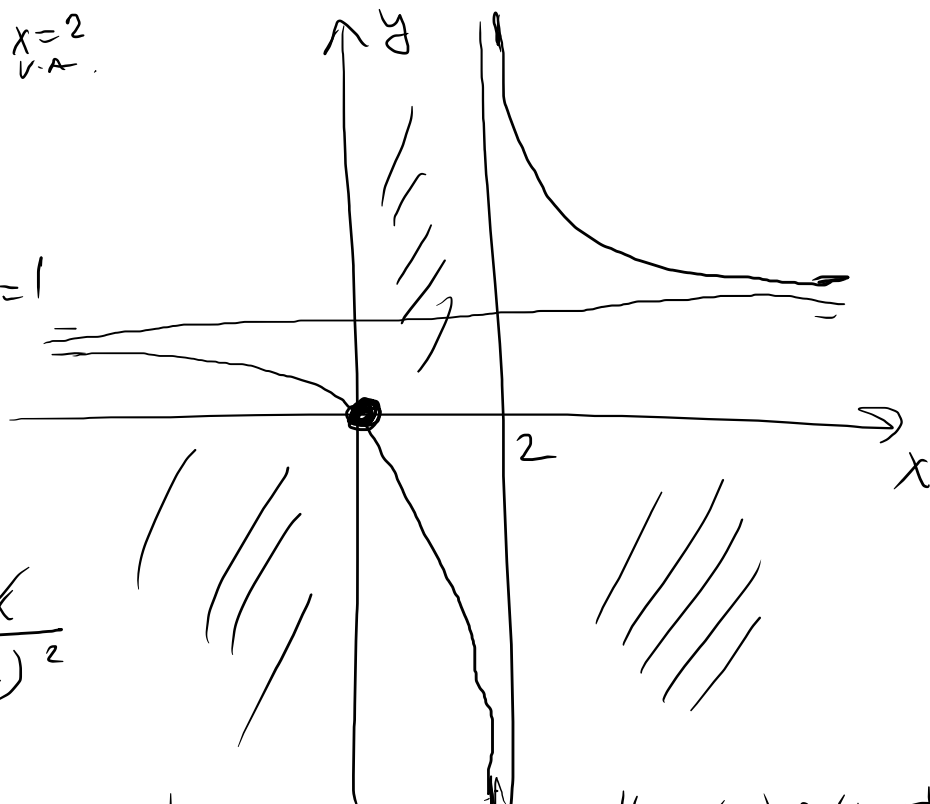
K.A. - keine
 für H.A.

$$6, y' = \frac{x-2-x}{(x-2)^2}$$

$$= \frac{-2}{(x-2)^2}$$

$$y' \neq 0 \quad \forall x \in \mathbb{R}$$

keine Determinante
 reduziert



$$y' < 0 \quad \forall x \in \mathbb{R}$$

$$y \searrow$$

$$7, y'' = \frac{-(-2) \cdot 2(x-2)}{(x-2)^3}$$

$$= \frac{4}{(x-2)^3} \quad y'' \neq 0 \quad \forall x \in \mathbb{R}$$

keine Wendepunkte
 fache
 $x-2 > 0 \quad y'' > 0 \quad x > 2$
 $x-2 < 0 \quad y'' < 0 \quad x < 2$